

TITE, Applied Mathematics

Ti5417700 Modelling methodology/T. Kauranne

Exercise 28.11.2006

1. Find the least squares fit for the parameters  $b_1, b_2$  of the model  $y = b_1(1 - e^{-b_2x})$  to the data  $x = (1, 3, 5, 7, 9), y = (0.076, 0.258, 0.369, 0.492, 0.559)$ . Use the FMINSEARCH optimizer.
2. To study the chemical reaction  $A + B \xrightarrow{k} C$  an experiment was performed using the initial concentrations  $A(0) = 0.054, B(0) = 0.106$ . The data below was measured:

% time	cA
426	0.0351
1150	0.0222
1660	0.0186
3120	0.0124

Estimate the value for the reaction rate constant  $k$ , when the reaction is given by the expression  $Re = kAB$ . Would a better fit be obtained by some of the forms  $Re = kA^mB^n$ , where  $m$  and  $n$  may get the values 1 or 2 ?

3. The chemical reaction  $A \xrightarrow{k_1} B \xrightarrow{k_2} C$  was started using the initial concentrations  $A(0) = 1, B(0) = C(0) = 0$ . Estimate the values for reaction rate constants, when the data below was measured:

! time	A	B
1.0e+00	5.04e-01	4.15e-01
2.0e+00	1.85e-01	4.88e-01
3.0e+00	2.17e-01	5.94e-01
4.0e+00	2.26e-02	5.05e-01
5.0e+00	1.01e-01	4.93e-01
6.0e+00	5.79e-02	4.57e-01
7.0e+00	6.45e-02	3.94e-01
8.0e+00	0.00e+00	3.34e-01
9.0e+00	8.20e-02	3.09e-01